## MATHSPACE

# mapping document 

This document outlines the mapping of Hong Kong Curriculum outcomes to particular topics and subtopics within Mathspace.

S1-S3
S4-S5

## S1-S3 Syllabus

| Number | Directed Numbers | Approximation and Error |
| :---: | :---: | :---: |
| Using a Calculator for Whole Number Mental Calculations Using a Calculator for Fractions Use a Calculator for Decimals Roman Numerals Egyptian Numbers Binary Number System Numbers with Different Bases | Representation of Directed Numbers <br> Integer Number Line <br> Comparing Sizes of Integers <br> Negative Number Placement and <br> Opposites <br> Comparisons of Directed Number Statements <br> Addition of Integers <br> Subtraction of Integers <br> Addition and Subtraction of Integers <br> Adjacent Signs <br> Multiplication of Integers <br> Division of Integers <br> Negative Squares and Cubes <br> Order of Operations <br> Order of operations with directed rational numbers <br> Mixed Problems with Directed Numbers <br> Using a Calculator for Directed Numbers | Significant Figures <br> Introducing Scientific Notation <br> Scientific Notation I <br> Using a Calculator for Scientific Notation <br> Scientific Notation II <br> Error in Measurement <br> Estimation and Rounding <br> Estimation with Decimals (Investigation) <br> Estimating Percentages <br> Checking Reasonableness and <br> Calculations |
| Perce | Interest and borrowing | Ratios and rates |
| Percentage of a Quantity <br> Percentage Composition <br> Percentage Change <br> Unitary Method <br> Best Buys and Discounts I <br> Best Buys and Discounts II <br> Business Applications of Percentages <br> Profit and Loss <br> Overtime and Extra Income <br> Commission and Other Income <br> Wages and Salaries <br> Wage Deductions and Net Income <br> Repeated Percentage Change <br> Deferred Payment Plans <br> Payment Methods <br> Using a Calculator with Percentages | Simple Interest <br> Compound Interest Introduction <br> Compound Interest - Compound <br> Variations <br> Compound Interest - Finding Other Values <br> Applicaions of Compound Interest - <br> Depreciation <br> Applications of Compound Interest - <br> Growth and Decay <br> Effective Interest Rates <br> Loans <br> Credit Cards | Introduction to Ratios <br> Simplifying Ratios <br> Problems Using Equivalent Ratios <br> Ratio Tables <br> Dividing a Quantity into a Given Ratio <br> Simplifying Ratios with Numeric Terms <br> Simplifying Ratios with Algebraic Terms <br> Ratios with Fractions and Percents <br> Decimal Ratios <br> Applications of Ratios <br> Ratios and Proportion <br> Dividing a Quantity into a Given Ratio <br> Scales, Maps and Ratios I <br> Scales, Maps and Ratios II <br> Rates I <br> Rates II |
| Number Patterns | Algebra I | Algebra II |
| Pictorial Representations of Algebra <br> Describing Number Patterns <br> Algebraic Expressions <br> Components in an expression <br> Laws of Arithmetic with Algebraic Terms <br> Substitution into Expressions <br> Algebraic Equations <br> Algebraic Conventions <br> Equivalent Expressions <br> Modelling Algebraic Expressions <br> Rules for Describing Sequences <br> Relationships between two Quantities <br> Table of values | Substitution into Algebraic Expressions I Worded Problems <br> Addition and subtraction of Like Terms <br> Directed Numbers in Algebra I <br> Equations <br> Directed Numbers in Algebra II <br> Substitution into Algebraic Expressions II <br> Substitution to Complete Table of Values <br> Substitution into common formulas <br> Formulas arising from Substitution <br> Addition and subtraction of Algebraic <br> Terms <br> Multiplication of Algebraic Terms <br> Division of Algebraic Terms <br> Algebraic Fractions I <br> Distributive Law <br> Factorizing the HCF <br> Rewriting Expressions <br> Equivalent Expressions <br> Multi-step word problems (arithmetic operations) <br> Multi-step word problems (averages and percentages) <br> Algebra in Measurement | Simplifying expressions with grouping symbols <br> Algebriac Fractions II <br> Algebraic Multiplication and Division <br> Using the Index Laws <br> Order of Operations I <br> Factorising Algebraic Factors <br> Problem Solving <br> Binomial Products <br> Order of Operations II <br> Factorising the HCF <br> Addition and Subtraction of Algebraic <br> Fractions <br> Multiplication and Division of Algebraic Fractions <br> Mixed Operations with Algebraic Fractions <br> Expanding Perfect Squares <br> Expanding Difference of two Squares Miscellaneous Expansions |


| Indices | Surds | Equations |
| :---: | :---: | :---: |
| Index Notation <br> The Zero Index <br> Multiplication Law I <br> Multiplication Law II <br> Division Law I <br> Division Law II <br> Power of a Power <br> Further Application of Index Laws <br> Negative Indices I <br> Numerical Bases with Negative Indices <br> Numerical Bases with Negative Indices (mult and division) <br> Numerical Bases with Negative Indices (power of power) <br> Numerical Bases with Negative Indices (mixed) <br> Mixed Index Laws <br> Negative Indices II <br> Multiplciation Law with Negative Indices <br> Division Law with Negative Indices <br> Power of Power with Negative Indices <br> Products and Quotients with Negative Indices | Rationals and Irrationals <br> Approximating Irrational Numbers <br> Answers that result in irrational numbers <br> Rational and Irrational Operations <br> Exact answers VS decimal evaluations <br> Simplifying Surds <br> Addition and Subtraction of Surds <br> Multiplication and Division of Surds <br> Rationalising the Denominator <br> Using a Calculator for Surds | Number Sentences <br> Introduction to Equations <br> Values that Satisfy Equations <br> Balancing Equations <br> Backtracking <br> Building Expressions Using Backtracking <br> One Step Equations <br> Two Step Equations <br> Number Problems <br> Problem Solving with Equations <br> Identifying Patterns <br> Simple Number Problems <br> Keeping Equations Balanced <br> Simple Equations <br> Three Step Equations <br> Variables on both sides I <br> Variables on both sides II <br> Problem solving with Equations <br> Solutions to Linear Equations <br> Comparing Linear Equations <br> Solve Equations with rational expressions <br> Equations involving Fractions <br> Formulae and Substitution <br> Changing the subject of a formula <br> Measurement Equations <br> Creating Equations with 1 Variable <br> Identities and Equations |
| Inequalities | Systems of Equations | Sequences |
| Introduction to Inequalities <br> One Step Inequalities <br> Two Step Inequalities <br> Problem Solving with Inequalities <br> Identifying Solutions to Inequalities in <br> Two Variables <br> Three Step Inequalities <br> Compound Inequalities\# | Introduction to Simulataneous Equations <br> The Graphical Method <br> The Substitution Method <br> The Elimination Method <br> Problems with Simultaneous Equations <br> Mixed Problems on Systems of Equations <br> Creating Inequalities with 2 Variables | Introduction to Sequences Introduction to Arithmetic Progressions Introduction to Geometric Progressions Fibonacci Sequence First Order Linear Recurrences Introduction |
| Linear Equations I | Linear Equations II | Factorization |
| The Number Plane <br> Interpreting Graphs <br> Horizontal and Vertical Lines <br> Identifying key features of Linear functions <br> Points on a Line <br> Intercepts <br> Graphing Straight Lines from Intercepts <br> Input and Output tables from Graphs <br> Finding the Rule <br> Identifying Linear Equations - Graphs <br> Graphing Linear Equations from Ordered Pairs <br> Solving Equations with Straight Lines Practical Linear Relationships | Unit Rates and Graphs <br> Comparing unit rates <br> Simple Proportional Relationships <br> Intercepts and The Intersection of Lines <br> Gradient of Horizontal and Vertical Lines <br> Gradient of a Line <br> Gradient from Two points <br> The Gradient Formula <br> Identifying Slope from Equation <br> Distances on the Plane (using Pythag) <br> The Distance Formula <br> The Midpoint of an Interval <br> Linear Relationships - graphs <br> Sketching Linear Graphs <br> Modelling Linear Relationships - graphs <br> Calculating Gradients <br> Parallel Lines I <br> Parallel Lines II <br> Perpendicular Lines <br> Intersections of Lines <br> Finding Linear Equations in Context <br> Geometrical Problems with Coordinates | Highest Common Factor <br> Difference of Two Squares <br> Perfect Squares <br> Grouping in Pairs <br> Monic Quadratic Trinomials <br> Miscellaneous Factorisations <br> Simplifying Algebraic Fractions <br> Factorising Algebraic Fractions (mult/div) <br> Factorising Algebraic Fractions (add/sub) <br> Complete the Square <br> Further Factorisations <br> Non-Monic Quadratic Trinomials <br> Factoring Sum and Difference of Cubes |


| Functions | Measuring, Estimating and Units |  |
| :---: | :---: | :---: |
| Describing functions <br> Defining Functions and Relations <br> Evaluating Functions <br> Polynomial curve sketching <br> Polynomials <br> Polynomials and Notation <br> Addition and Subtraction of Polynomials <br> Multiplication of Polynomials | Units to measure capacity, mass and length <br> Appropriate Units <br> Units of capacity I <br> Units of Capacity II <br> Appropriate Volume and Capacity Units <br> Units of Mass I <br> Units of Mass II <br> Units of Mass III <br> Appropriate Units of Mass <br> Units of Length <br> Units of Measurement <br> Units of Area Conversions <br> Measure and estimate length of objects <br> Estimate Lengths <br> Measure and estimate mass of objects <br> Measure and estimate capacity of objects | Measure, estimate, order and compare objects <br> Measure, estimate, order and compare temperature <br> Estimate Area <br> Estimate Volume <br> Mixed Unit Conversions <br> Units resulting from a formula or graph <br> Quantities, Units and Modelling <br> Reasonable Units <br> Converting Units Very large and small <br> Accuracy in Measurement (upper and lower bounds) <br> Accuracy and Precision <br> Error in Measurement <br> Dimensional analysis (construction of units) |
| Measurement | Trigonometry | Geometry |
| Perimeter I <br> Perimeter II <br> Introduction to Area <br> Area of Rectangles and Squares <br> Area of Triangles <br> Area of Parallelograms <br> Area of Composite Shapes I <br> Area of Composite Shapes II <br> Exploring the area of special quadrilaterals <br> Area of Special Quadrilaterals <br> Connecting Perimeters and Areas <br> Area of Non Right Angle Triangles <br> Parts of a Circle <br> Circumference <br> Area of a Circle <br> Area and Perimeter of Sectors <br> Volume of Rectangular Prisms <br> Volume <br> Volume of Prisms I <br> Volume of Prisms II <br> Volume of Cylinders I <br> Volume of Cylinders II <br> Volume of Right Pyramids <br> Volume of Right Cones <br> Volume of Spheres <br> Volume of Composite Solids I <br> Volume of Composite Solids II <br> Applications of Volume <br> Surface Area of Prisms I <br> Surface Area of Prisms II <br> Surface Area of Cylinders I <br> Surface Area of Cylinders II <br> Surface Area of Right Pyramids and Cones <br> Surface Area of a Sphere <br> Surface Area of Simple Composite Solids <br> Surface Area of Composite Solids <br> Surface Area of Complex Composite Solids | PYTHAG - The Right-Angled Triangle <br> PYTHAG - Pythagorean Triads <br> PYTHAG - Calculating Side Lengths Using <br> Pythagoras <br> PYTHAG - Applications using Pythagoras <br> PYTHAG - Review (calculations and applications) <br> Sides of a Right-Angled Triangle <br> Ratio of Sides in Right-Angled Triangles <br> Trigonometric Ratios I <br> Trigonometric Ratios II <br> Trigonometric Ratios with Exact Values <br> Calculating Trigonometric Expressions <br> Finding Unknown Side Lengths Using Trig Ratios <br> Finding Unknown Angles <br> Triangle Problems <br> Applications to Geometry <br> Angles of Elevation and Depression <br> Problems with Two Right-Angled Triangles <br> Applications to Real Life I <br> Applications to Real Life II <br> Trigonometry in 3D <br> Pythagoras in $3 \mathrm{D}^{\#}$ <br> Applications Including Bearings <br> Exact Trigonometric Values <br> Trigonometric Equations - with Exact Values <br> Trigonometric Equations - Complimentary <br> Results and Ratios | Polygons <br> Classification of Solids <br> Faces, Edges and Vertices in Polyhedra <br> Nets of solids <br> Naming Angles <br> Measuring, Estimating and Drawing Angles <br> Angles at a Point \& vertically Opposite Angles <br> Types of Triangles <br> Types of Quadrilaterals <br> Symmetry <br> Lengths in Polygons on the Plane <br> Constructing 3D Shapes (Investigation) <br> Visualising Solids <br> Cross Sections of Prisms <br> Lines, Intervals and Rays <br> Angles on a straight line <br> Complementary and Supplementary Angles <br> Angles in Triangles <br> Interior and Exterior Angles of Polygons <br> Exterior Angle Sum and other Calculations <br> Cointerior Angles <br> Alternate Angles <br> Corresponding Angles <br> Angles and Parallel Lines <br> Identifying Parallel Lines <br> Constructions with a compass <br> Angles in Quadrilaterals <br> Lengths in Quadrilaterals <br> Properties of Quadrilaterals <br> Identifying Polygons from angle conditions <br> Drawing and Recognising Shapes with <br> Properties (Investigation) <br> Triangle problems <br> Angles in Triangles Revision <br> Angles and Lengths in Quadrilaterals Revision <br> Shapes in Fractal Geometry <br> Symmetries in 3-D Shapes <br> Soma Cubes <br> Angles on Parallel Lines Revision <br> Harder Angles on Parallel Lines <br> Centres of Triangles\# <br> Geometrical Calculations <br> Deductive Proofs <br> Proofs with Triangles <br> Proofs with Quadrilaterals |


| Congruence and Similarity | Probability | Data Analysis |
| :---: | :---: | :---: |
| Translations on the Cartesian Plane <br> Reflections on the Cartesian Plane <br> Rotations on the Cartesian Plane <br> Combined Transformations on the <br> Cartesian Plane <br> Tesselations <br> Line and Rotational Symmetries <br> Introduction to Congruence <br> Transformations and Congruence <br> Congruence in Triangles <br> Congruence in Quadrilaterals <br> Simple Proofs for Congruence in Triangles <br> Find sides and angles with congruent relationships <br> Methods for Enlargements <br> Enlargements, Ratio and Scale Factors <br> Introduction to Similarity <br> Transformations and Similarity <br> Similarity in Triangles <br> Using similarity proportion to solve problems <br> Trigonometry and Similarity <br> Conditions of Similarity <br> Area and Volumes of Similar Figures | Range of Probabilities <br> Describing Chance <br> Sample Spaces <br> Probabilities as Rational Number <br> Conducting Experiments (Investigation) <br> Experimental Probability <br> Theoretical Probability <br> Expected Outcomes <br> Generating data for probability analysis (Investigation) <br> Venn Diagrams and Two Way Tables <br> Complementary Events <br> Describing and/or events <br> Relative frequencies of And/Or events <br> tree diagrams <br> Replacement and non-replacement probabilities <br> Using Frequency tables and graphs to estimate probabilities <br> Expectation and Fair Value <br> Mixed Questions on Probability <br> Probabilities of Games <br> Traffic Light Problems <br> Decision Making using Probability (Investigation) <br> Comparisons from Experiments (Investigation) | Types of Data I <br> Practicalities of Obtaining Data <br> Statistical Questions <br> Frequency Tables <br> Grouped Data <br> Number of Observations <br> Statistical Attributes <br> Line, Conversion and Step Graphs <br> Stem and Leaf Plots <br> Dot Plots <br> Create and interpret column or bar graphs <br> Create and Interpret Histograms <br> Travel Graphs <br> Sector Graphs <br> Divided Bar Graphs <br> Area Charts and Radar Graphs <br> Back to back stem and leaf plots <br> Histograms and Polygons <br> The Mean <br> The Median <br> Mode <br> Range <br> Mean, Median, Mode and Range <br> Centre or Spread ? <br> How the shape affects choice of centre and spread <br> Weighted Means <br> Cumulative Frequency <br> Frequency Distribution for Grouped Data <br> Measures of Spread - Quartiles <br> Comparisons and Predictions <br> Comparing Sets of Data I <br> Comparing Sets of Data II <br> Real Life Data I <br> Real Life Data II <br> Statistics in the Media I <br> Statistics in the Media II <br> Scatter Plots <br> Describing Statistical Relationships <br> Step graphs <br> Statistical Investigations |


| Number and Number Systems |  |  |
| :---: | :---: | :---: |
| Directed Numbers and the Number Line |  |  |
| understand and accept intuitively the concept and uses of negative numbers | Directed Numbers | Representation of Directed Numbers Comparisons of Directed Number Statements |
| have simple ideas of ordering on the number line | Directed Numbers | Integer Number Line <br> Comparing Sizes of Integers <br> Negative Number Placement and Opposites\# <br> Comparisons of Directed Number Statements |
| explore and discuss the manipulation of directed numbers | Directed Numbers | Negative Number Placement and Opposites\# <br> Comparisons of Directed Number Statements <br> Addition of Integers <br> Subtraction of Integers <br> Addition and Subtraction of Integers <br> Adjacent Signs <br> Multiplication of Integers <br> Division of Integers <br> Mixed Problems with Directed Numbers |
| manipulate directed numbers | Directed Numbers | Addition of Integers <br> Subtraction of Integers <br> Addition and Subtraction of Integers <br> Adjacent Signs <br> Multiplication of Integers <br> Division of Integers <br> Negative Squares and Cubes <br> Order of Operations <br> Order of operations with directed rational numbers <br> Mixed Problems with Directed Numbers |
| Numerical Esimation |  |  |
| be aware of the need to use estimation strategies in real-life situations and appreciate the past attempts to approximate values such as $\pi$ | Approximation and Errors | Estimation (Investigation) ${ }^{\text {\# }}$ |
| determine whether to estimate values or to compute the exact values | Surds | Approximating Irrational Numbers Exact Answers vs Decimal Evaluations |
| select and use estimation strategies to estimate values and to judge the reasonableness of results | Approximation and Errors | Estimation and Rounding Checking Reasonableness and Calculations Estimation with Decimals (Investigation) Estimating Percentages |
| choose appropriate means for calculation such as mental computation, calculators or paper and pencil etc. | Number <br> Directed Number | Mental Calculations <br> Using a Calculator for Whole Number <br> Using a Calculator for Fractions <br> Using a Calculator for Decimals <br> Using a Calculator for Directed Numbers |


| Approximation and Errors |  |  |
| :---: | :---: | :---: |
| acquire further concepts and skills of rounding off numbers to a required number of significant figures | Approximation and Errors | Significant Figures |
| understand the meaning of scientific notation | Approximation and Errors | Introducing Scientific Notation |
| use scientific notation in practical problems | Approximation and Errors | Scientific Notation I <br> Scientific Notation II <br> Using a Calculator for Scientific Notation |
| be aware of the size of errors during estimation and approximation | Approximation and Errors | Errors in Measurement |
| understand and calculate different types of errors such as absolute errors, relative errors and percentage errors | Approximation and Errors | Errors in Measurement |
| Rational and Irrational Numbers |  |  |
| be aware of the existence of irrational numbers and surds | Surds | Rationals and Irrationals <br> Answers that result in irrational numbers <br> Rational and Irrational Operations <br> Exact Answers VS Decimal Evaluations |
| explore the representations of irrational numbers in the number line | Surds | Approximating Irrational Numbers |
| (NF) manipulate commonly encountered surds including the rationalization of the denominator in the form of Va | Surds | Addition and subtaction of Surds Multiplication and Division of Surds Rationalising the Denominator |
| (NF) appreciate the expressions of surds could be expressed in a more concise form | Surds | Simplifying Surds <br> Addition and subtaction of Surds <br> Multiplication and Division of Surds |
| Comparing Quantities |  |  |
| Using Percentages |  |  |
| understand the meaning of percentages and percentage changes | Percentages | Percentage of a Quantity Percentage Composition Percentage Change |
| apply percentage changes to solve simple selling problems | Percentages <br> Interest and Borrowing | Unitary Method <br> Business Applications of Percentages <br> Best Buys and Discounts I \& II <br> Deferred Payment Plans <br> Payment Methods <br> Simple Interest |
| apply percentages to solve problems involving simple and compound interests, growth and depreciation | Interest and Borrowing | Compound Interest Introduction <br> Compound Interest - Compound Variations <br> Compound Interest - Finding Other Values <br> Applicaions of Compound Interest - Depreciation <br> Applications of Compound Interest - Growth and Decay |
| More About Percentages |  |  |
| apply percentages to solve further practical problems involving successive and component changes | Percentages | Repeated Percentage Change |
| apply percentages to solve simple real-life problems involving taxation and rates | Percentages <br> Interest and Borrowing | Wages and Salaries <br> Commission and Other Income <br> Profit and Loss <br> Overtime and Extra Income <br> Wage Deductions and Net Income <br> Effective Interest Rates <br> Loans <br> Credit Cards |


| Rate and Ratio |  |  |
| :--- | :--- | :--- |
| understand the meaning of rate and ratio | Ratios and Rates | Introduction to Ratios and Rates <br> Ratio Tables <br> Rates I \& II |
| recognize the notation of a : b, a : b:c |  | Ratios and Rates |
|  |  | Introduction to Ratios and Rates <br> Ratio Tables <br> Simplifying Ratios |


| formulate simple algebraic equations/ inequalities to solve problems | Number Patterns <br> Algebra I <br> Algebra II Equations <br> Inequalities | Algebraic Equations <br> Equations <br> Multi-step word problems (arithmetic operations) <br> Multi-step word problems (averages and percentages) <br> Problem Solving <br> Number Sentences <br> Introduction to Equations <br> Values that Satisfy Equations <br> Balancing Equations <br> Backtracking <br> Building Expressions Using Backtracking <br> One Step Equations <br> Two Step Equations <br> Number Problems <br> Problem Solving with Equations <br> Introduction to Inequalities <br> One Step Inequalities <br> Two Step Inequalities <br> Creating Inequalities with 2 Variables |
| :---: | :---: | :---: |
| investigate, appreciate and observe the patterns of various number sequences such as polygonal numbers, arithmetic and geometric sequences, Fibonacci sequence etc. | Sequences | Introduction to Sequences <br> Introduction to Arithmetic Progressions <br> Introduction to Geometric Progressions <br> Fibonacci SequenceIntroduction to Sequences <br> First Order Linear Recurrences Introduction |
| use algebraic symbols to represent the number patterns | Number Patterns <br> Algebra I | Modelling Algebraic Expressions Rules for Describing Sequences Table of Values Worded Problems |
| obtain a preliminary idea of function such as input-processing-output concept | Number Patterns Linear Equations I <br> Functions | Relationships between Two Quantities Input and Output tables from graphs Finding the ruel Evaluating functions |
| Manipulations of Simple Polynomials |  |  |
| recognize polynomial as a special example of algebraic expressions | Polynomials | Polynomials and Notation |
| recognize the meaning of the terminology involved | Functions <br> Polynomials | Describing Functions <br> Defining Functions and Relations <br> Evaluating functions <br> Polynomials and Notation |
| add, subtract, multiply polynomials involving more than one variable | Polynomials | Addition and Subtraction of Polynomials Multiplication of Polynomials |
| Laws of Integral Indices |  |  |
| extend and explore the meaning of the index notation of numbers with negative exponents | Indices | Negative Indices I \& II <br> Numerical Bases with Negative Indices <br> Numerical Bases with Negative Indices (mult and division) <br> Numerical Bases with Negative Indices (power of power) <br> Numerical Bases with Negative Indices (mixed) <br> Mixed Index Laws <br> Negative Indices <br> Multiplciation Law with Negative Indices <br> Division Law with Negative Indices <br> Power of Power with Negative Indices <br> Products and Quotients with Negative Indices |
| explore, understand and use the laws of integral indices to simplify simple algebraic expressions (up to 2 variables only) | Algebra II | Algebraic Multiplication and Division Using the Index Laws |


| (NF) understand and compare numbers expressed in various bases in real-life situations | Number | Numbers with Different Bases |
| :---: | :---: | :---: |
| (NF) foster a sense of place values in different numeral systems | Number | Roman Numerals Egyptian Numbers Binary Number System |
| (NF) inter-convert between simple binary/hexadecimal numbers to decimal numbers | Number | Numbers with Different Bases |
| Factorization of Simple Polynomials |  |  |
| understand factorization as a reverse process of exapnsion | Algebra I <br> Algebra II <br> Factorization | Distributive Law <br> Factorising the HCF <br> Simplifying Expressions with Grouping Symbols <br> Binomial Products <br> Difference of Two Squares <br> Perfect Squares |
| factorize polynomials by using common factors and grouping of terms | Algebra I <br> Algebra II <br> Factorization | Factorising the HCF <br> Factorising the HCF <br> Factorising Algebriac Factors <br> Highest Common Factor <br> Grouping in Pairs |
| factorize polynomials by using identifies including difference of two squares; perfect square expressions; difference and sum of two cubes (NF - difference and sum of two cubes) | Factorization | Difference of Two Squares <br> Perfect Squares <br> Monic Quadratic Trinomials <br> Micellaneous Factorisations <br> Further Factorisations <br> Complete the Square <br> Factoring sum and difference of cubes |
| factorize polynomials by cross-method | Factorization | Monic Quadratic Trinomials Non-Monic Quadratic Trinomials |
| Algebraic Relations and Functions |  |  |
| Linear Equations in One Unknown |  |  |
| formulate and solve linear equations in one unknown | Equations | One Step Equations <br> Two Step Equations <br> Number Problems <br> Problem Solving with Equations <br> Identifying Patterns <br> Simple Number Problems <br> Keeping Equations Balanced <br> Simple Equations <br> Three Step Equations <br> Grouping with Pronumerals I \& II <br> Problem solving with Equations <br> Solutions to Linear Equations <br> Comparing Linear Equations <br> Solve Equations (add/sub) with rational expressions <br> Solve Equations (mult) with rational expressions <br> Solve Equations (div) with rational expressions <br> Equations involving Fractions <br> Formulae and Substitution <br> Measurement Equations <br> Creating Equations with 1 Variable |
| **solve literal equations | Equations | Changing the subject of a formula |


| Linear Equations in Two Unknowns |  |  |
| :--- | :--- | :--- |
| plot and explore the graphs of linear <br> equations in 2 unknowns | Linear Equations I | Interpreting Graphs <br> Horizontal and Vertical Lines <br> Points on a Line |


| solve simple linear inequalities in one <br> unknown and represent the solution on the <br> number line |  | Inequalities |
| :--- | :--- | :--- | | One Step Inequalities |
| :--- |
| Two Step inequalities |
|  |
|  |
| Problem Solving with Inequalities |
| Identifying Solutions to Inequalities |

## Measures in 2-D and 3-D Figures

| Estimation in Measurement |  |  |
| :---: | :---: | :---: |
| recognize the approximate nature of measurement and choose an appropriate measuring tool and technique for a particular purpose | Measuring Estimating and Units | Accuracy and Precision |
| choose an appropriate unit and the degree of accuracy for a particular purpose | Measuring, Estimating and Units | Units to measure capacity, mass and length <br> Appropriate Units <br> Units of capacity I \& II <br> Appropriate Volume and Capacity Units <br> Units of Mass I, II and III <br> Appropriate Units of Mass <br> Units of Length <br> Units of Measurement <br> Units of Area Conversions <br> Mixed Unit Conversions <br> Units resulting from a formula or graph <br> Quantities, Units and Modelling <br> Reasonable Units <br> Converting Units Very large and small |
| develop estimation strategies in measurement | Measuring, Estimating and Units | Measure ad Estimate Length of Objects <br> Estimate Lengths <br> Measure and Estimate Mass of Objects <br> Measure and Estimate capacity of objects <br> Measure, estimate, order and compare objects <br> Measure, estimate, order and compare temperature <br> Estimate Area <br> Estimate Volume |
| handle and reduce errors in measurement | Measuring, <br> Estimating and Units | Accuracy in Measurement (upper and lower bounds) <br> Accuracy and Precision <br> Error in Measurement |
| estimate, measure and calculate lengths, areas, capacities, volumes, weights, rates, etc. | Measuring, Estimating and Units <br> Measurement | Measure ad Estimate Length of Objects <br> Estimate Lengths <br> Measure and Estimate Mass of Objects <br> Measure and Estimate capacity of objects <br> Measure, estimate, order and compare objects <br> Measure, estimate, order and compare <br> temperature <br> Estimate Area <br> Estimate Volume <br> Perimeter I \& II <br> Area of Rectangles and Squares <br> Area of a Triangles <br> Area of Parallelograms <br> Area of Composite Shapes I <br> Area of Composite Shapes II <br> Area of Special Quadrilaterals |

\(\left.$$
\begin{array}{|ll|l|}\hline \text { Simple Ideas of Areas and Volumes } & & \\
\hline \text { find areas of simple polygons } & \text { Measurement } & \begin{array}{l}\text { Introduction to Area } \\
\text { Area of Rectangles and Squares } \\
\text { Area of a Triangles }\end{array}
$$ <br>

Area of Parallelograms\end{array}\right]\)| Area of Composite Shapes I |
| :--- |
| Area of Composite Shapes II |
| Exploring the area of special quadrilaterals |
| Area of Special Quadrilaterals |

Learning Geometry Through an Intuitive Approach

| Introduction to Geometry |  |  |
| :--- | ---: | :--- |
| recognize the common terms and notations <br> in geometry such as line segments, angles, <br> regular polygons, cubes and regular <br> polyhedra (Platonic solids) etc. | Geometry | Polygons <br> Lines, Intervals and Rays |
| identify types of angles and polygons |  | Geometry | | Polygons |
| :--- |
| Classification of Solids |


| bisectors and special angles by compasses <br> and straight edges |  |  |
| :--- | :--- | :--- |
| (NF) appreciate the construction of lines and <br> angles with minimal tools at hand | Geometry | Constructions with a compass <br> Measring, Estimating and Drawing Angles |
| ** discuss the possibility of trisecting an <br> angle by compasses and straight edges | Geometry | Constructions with a Compass |
| **explore some shapes in fractal geometry | Geometry | Introduction to Fractal Geometry |
| Angles related with Lines and Rectilinear Figures |  | Geometry | | Naming Angles |
| :--- |
| recognize different types of angles |

Learning Geometry through a Deductive Approach

## Simple Introduction to Deductive Geometry

| develop a deductive approach to study geometric properties through studying the story of Euclid and his book - Elements |  | Investigation coming |
| :---: | :---: | :---: |
| develop an intuitive idea of deductive reasoning by presenting proofs of geometric problems relating with angles and lines | Geometry | Geometrical Calculations <br> Deductive Proofs <br> Proofs with Triangles <br> Proofs with Quadrilaterals |
| understand and use the conditions for congruent and similar triangles to perform simple proofs | Congruence and Similarity | Simple Proofs for Congruence in Triangles Find sides and angles with congruent relationships Congruence in Triangles |
| identify lines in a triangle such as medians, perpendicular bisectors etc. | Geometry | Centres of Triangles\# |
| (NF) explore and recognize the relations between the lines of triangles such as the triangle inequality, concurrence of intersecting points of medians etc. | Geometry | Centres of Triangles\# |
| (NF) explore and justify the methods of constructing centres of a triangle such as incentre, circumcentre, orthocentre, centroids etc. | Geometry | Centres of Triangles\# |
| ** prove some properties of the centres of the triangle | Geometry | Centres of Triangles\# |
| Pythagoras' Theorem |  |  |
| recognize and appreciate different proofs of Pythagoras' Theorem including those in Ancient China |  | Investigation coming |
| recognize the existence of irrational numbers and surds | Surds | Rationals and Irrationals <br> Answers that result in irrational numbers |
| use Pythagoras' Theorem and its converse to solve problems | Trigonometry | PYTHAG - The Right-Angled Triangle <br> PYTHAG - Pythagorean Triads <br> PYTHAG - Calculating Side Lengths Using <br> Pythagoras <br> Pythagoras in 3D\# <br> PYTHAG - Applications Using Pythagoras <br> PYTHAG - Review |
| (NF) appreciate the dynamic element of mathematics knowledge through studying the story of the first crisis of mathematics |  | Investigation coming |
| **investigate and compare the approaches behind in proving Pythagoras' Theorem in different cultures |  | Investigation coming |
| **explore various methods in finding square root |  | Investigation coming |
| Quadrilaterals |  |  |
| extend the idea of deductive reasoning in handling geometric problems involving quadrilaterals | Geometry | Angles in Quadrilaterals Lengths in Quadrilaterals Properties of Quadrilaterals Proofs with Quadrilaterals |
| deduce the properties of various types of quadrilaterals but with focus on parallelograms and special quadrilaterals | Geometry | Types of Quadrilaterals Lengths in Polygons on the Plane \# Identifying Polygons from angle conditions\# Angles and Lengths in Quadrilaterals Revision |
| (NF) perform simple proofs related with parallelograms | Geometry Congruence and Similarity | Proofs with Quadrilaterals <br> Congruence in Quadrilaterals \# <br> Using similarity proportion to solve problems \# |

(NF) understand and use the mid-point and
Investigation coming intercept theorems to find unknowns

## Learning Geometry through an Analytic Approach

| Introduction to Coordinates |  |  |
| :---: | :---: | :---: |
| understand and use the rectangular and polar coordinate systems to describe positions of points in a plane | Linear Equations I | The Number Plane |
| able to locate a point in a plane by means of an ordered pair in the rectangular coordinate system | Linear Equations I | The Number Plane Graphing straight lines from ordered pairs |
| describe intuitively the effects of transformation such as translation, reflection with respect to lines parallel to $x$ axis, $y$-axis and rotation about the origin through multiples of $90^{\circ}$ on points in coordinate planes | Congruence and Similarity | Translations on the Cartesian Plane <br> Reflections on the Cartesian Plane <br> Rotations on the Cartesian Plane <br> Combined Transformations on the Cartesian Plane |
| calculate areas of figures that can be cut into or formed by common 2-D rectilinear figures | Measurement | Area of Composite Shapes I \& II |
| Coordinate Geometry of Straight Lines |  |  |
| understand and use formulas of distance and slope | Linear Equations II | Gradient of Horizontal and Vertical Lines <br> Gradient of a Line <br> Gradient from Two Points <br> The Gradient Formula <br> Identifying Slope from Equation <br> Distances on the plane (using pythag0 <br> The Distance Formula <br> The Midpoint of an Interval <br> Calculating Gradients <br> Finding Linear Equations in Context <br> Geometrical Problems with Coordinates |
| (NF) use ratio to find the coordinates of the internal point of division and mid-point | Linear Equations II | The Midpoint of an Interval |
| understand the conditions for parallel lines and perpendicular lines | Linear Equations II | Parallel Lines II Parallel Lines II Perpendicular Lines |
| (NF) appreciate the analytic approach to prove results relating to rectilinear figures besides deductive approach |  | Investigation coming |
| (NF) choose and use appropriate methods to prove results relating to rectilinear figures |  | Investigation coming |
| **explore the formula for external point of division |  | Investigation coming |
| Trigonometry |  |  |
| Trigonometric Ratios and Using Trigonometry |  |  |
| understand the sine, cosine and tangent ratios for angles between $0^{\circ}$ to $90^{\circ}$ | Trigonometry | Sides of a Right-Angled Triangle <br> Ratio of Sides in Right-Angled Triangles <br> Trigonometric Ratios I <br> Trigonometric Ratios II <br> Trigonometric Ratios with Exact Values <br> Calculating Trigonometric Expressions <br> Finding Unknown Side Lengths Using Trig Ratios <br> Finding Unknown Angles <br> Triangle Problems <br> Applications to Geometry <br> Applications to Real Life I <br> Applications to Real Life II |

\(\left.$$
\begin{array}{|l|l|l|}\hline \begin{array}{l}\text { explore the properties and relations of } \\
\text { trigonometric ratios }\end{array} & \text { Trigonometry } & \begin{array}{l}\text { Sides of a Right-Angled Triangle } \\
\text { Ratio of Sides in Right-Angled Triangles } \\
\text { Trigonometric Ratios I }\end{array} \\
\hline & & \begin{array}{l}\text { Trigonometric Ratios II }\end{array}
$$ <br>
Trigonometric Ratios with Exact Values <br>

Calculating Trigonometric Expressions\end{array}\right]\)| Finding Unknown Side Lengths Using Trig Ratios |
| :--- |
| Finding Unknown Angles |, | Triangle Problems |
| :--- |

\(\left.$$
\begin{array}{|l|l|l|}\hline \text { Organization and Representation of Data } & & \\
\hline \text { Introduction to Various Stages of Statistics } & & \\
\hline \text { recognize various stages involved in statistics } & \text { Data Analysis } & \text { Statistical Investigations } \\
\hline \begin{array}{l}\text { use simple methods to collect data so as to } \\
\text { analyze posed problems }\end{array} & & \text { Data Analysis }\end{array}
$$ \begin{array}{l}Practicalities of Obtaining Data <br>

Statistical Questions\end{array}\right]\)| Number of Observations |
| :--- | :--- |
| Statistical Attributes |

\(\left.$$
\begin{array}{|l|l|l|}\hline \begin{array}{l}\text { use some common wordings such as 'most } \\
\text { popular', 'most likely', 'equally likely' to describe } \\
\text { trends from line graphs }\end{array} & & \text { Investigation coming } \\
\hline \begin{array}{l}\text { discuss the impressions from graphs presented in } \\
\text { various sources }\end{array} & \text { Data Analysis } & \begin{array}{l}\text { Statistics in the Media I } \\
\text { Statistics in the Media II }\end{array} \\
\hline \begin{array}{l}\text { identify sources of deception in misleading } \\
\text { graphs and their accompanying statements }\end{array} & & \text { Data Analysis }\end{array}
$$ \begin{array}{l}Comparisons and Predictions <br>
Comparing Sets of Data I <br>
Comparing Sets of Data II <br>
Real Life Data I <br>
Real Life Data II <br>
Statistics in the Media I <br>

Statistics in the Media II\end{array}\right]\)


| Probability |  |  |
| :---: | :---: | :---: |
| Simple Idea of Probability |  |  |
| explore the meaning of probability through various activities | Probability | Describing Chance <br> Experimental Probability Generating data for probability analysis Venn diagrams and two way tables Describing and/or events Tree diagrams |
| have an intuitive idea about the relation between probability and the relative frequency as found in statistics or simulation activities | Probability | Probabilities as rational number <br> Theoretical Probability <br> Generating data for probability analysis <br> Complementary Events <br> Relatvie frequencies of And/Or events <br> Expectation and Fair Value |
| investigate probability in real-life activities, including geometric probability | Probability | Conducting Experiments (investigation) <br> Probabilities of Games <br> Traffic Light Problems <br> Decision Making using Probability <br> (Investigation) <br> Comparisions from Experiments (Investigation) |
| compare the empirical and theoretical probabilities | Probability | Theoretical Probability Expected Outcomes |
| calculate the theoretical probability by listing the sample space and counting | Probability | Sample Spaces <br> Theoretical Probability <br> Replacement and non-replacement <br> probabilities <br> Using Frequency tables and graphs to estimage probabilities <br> Mixed Questions on Probability |
| recognize the meaning of expectation | Probability | Expected Outcomes |
| Included as Background and Supporting Work |  |  |
| Whilst not explicitly required as part of the curriculum, these subtopics are included for background and supporting work for the benefit it can add to student learning and understanding | Data Analysis | Divided Bar Graphs <br> Area Charts and Radar Graphs |

## S4-S5 Syllabus

| Number and Algebra Review | Proportions | Indices |
| :---: | :---: | :---: |
| Whole Number Review <br> Fraction Review <br> Decimal Review <br> Recurring Decimals as/from Fractions <br> Converting Recurring Decimals to <br> Fractions <br> Percentage Review <br> Ratios and Rates Review <br> Algebra Review <br> Probability Review | Proportional Relationships <br> Constant of Proportionality <br> Proportional Relationships as Equations <br> Interpreting Proportional Relationships <br> Graphs and Direct Proportions <br> Direct Proportion | Numerical Bases with Fractional Indices Fractional Bases with Fractional Indices Fractional Indices with Algebraic Terms |
| Equations | Inequalities | Linear Equations I |
| Mixed Equations I <br> Mixed Equations II <br> Problem Solving with Linear and Non- <br> Linear Equations <br> Simple Exponential Equations <br> Solving Cubic Equations <br> Identify Solutions to Linear Equations <br> Solving Equations through Trial and Improvement <br> Solve Radical Equations <br> Solve Equations with Rational Expressions <br> Solve Equations with Negative Exponents\# <br> Solve Equations with Nested Radicals\# | Introduction to Inequalities <br> One Step Inequalities <br> Two Step inequalities <br> Problem Solving with Inequalities <br> Identifying Solutions to Inequalities in <br> Two Variables <br> Three step Inequalitites <br> Compound Inequalities\# <br> Solve Linear Inequalities from a Graph ${ }^{\#}$ <br> Solve polynomial inequalities\# <br> Graphing Linear and Non-Linear Inequalities <br> Constructing Inequalities or Systems of Inequalities <br> Systems of Inequalities in Two Variables <br> Creating Inequalities with 2 Variables <br> Problems with Systems of Inequalities in 2 Variables | Identifying key features of Linear functions <br> Identifying Slope from Equation <br> Gradient-Intercept Form <br> Equation of a Line: General Form <br> The Point Slope Formula <br> The Two Point Formula <br> Equations of Lines (Mixed Set) <br> Finding the Rule <br> Linear Relationships - graphs <br> Sketching Linear Graphs <br> Linear functions, summary of features <br> Modelling Linear Relationships - graphs <br> Direct Proportion <br> Inverse Proportion <br> Finding the Equation of Line <br> Graphs of Physical Phenomena |
| Linear Equations II | Quadratic Equations |  |
| Linear modelling <br> Linear modelling- Simultaneous Equations <br> Linear Modelling - Break Even Analysis <br> Linear Programming - Graphical Method\# <br> Linear Programming - Objective Function\# <br> Linear Programming - Feasible Regions\# <br> Linear Programming - Applications\# <br> Writing Intervals \# <br> Division of an interval in a given ratio <br> Perpendicular distance ${ }^{\#}$ <br> Angle between two lines\# <br> Proportion and Variation | Quadratic relationship <br> Transformations and Quadratic Equtions <br> Transformation and Quadratic Graphs <br> Identifying Key Features of Quadratics <br> Solving basic quadratic equations <br> Solve by Factorisation I <br> Graphing Quadratic Functions in <br> Factorised Form <br> Solving by factorisation II <br> Solving by completing the square I <br> Graphing Quadratic Functions in Turning Point Form | Graphing Quadratic Functions in General Form <br> Variable substitution Method <br> The Number and Nature of Solutions <br> Simultaneous, linear and quadratic equations <br> Applications of Quadratic Functions using graphs <br> Further Applications <br> Solve fractional equations that result in quadratics <br> Quadratic Graphing Review |
| Factorisation | Using Vertex Formula | Sum and product of roots |
| Highest Common Factor <br> Difference of Two Squares <br> Perfect Squares <br> Grouping in Pairs <br> Monic Quadratic Trinomials <br> Miscellaneous Factorisations <br> Factorising Algebraic Fractions (mult/div) <br> Factorising Algebraic Fractions (add/sub) <br> Complete the Square <br> Non-Monic Quadratic Trinomials <br> Factoring Sum and Difference of Cubes | Solving using the quadratic formula <br> Application Problems <br> Miscellaneous Equations <br> Solving by completing the square II <br> NonMonic Quadraitc Equations | Quadratic Identities\# <br> Maximum and Minimum Values of Quadratic Equations <br> Applications of Maximisation and Minimisation <br> Solve Quadratic Inequalities\# |
| Power Functions | Cubic Functions | Functions (Theory of) |
| Power Functions <br> Solving for Constant of Proportionality in Power Functions | Graphing Cubic Functions <br> Factoring Cubics with an identifiable factor <br> Solve applications involving cubic functions <br> Solve Inequalities involving Cubics Evaluating Cubic and Other Power Functions | Describing functions <br> Defining Functions and Relations Identifying One-to-One Functions <br> Evaluating Functions <br> Odd and Even Functions <br> Algebra of Functions |


| Simple Rational Functions | Hyperbolic Functions | Parabolic Functions |
| :---: | :---: | :---: |
| Identify Characteristics of Simple Rational Functions <br> Transformations of Simple Rational Functions Graphing Simple Rational Functions | Identify Characteristics of Hyperbolic Functions\# <br> Graphing Hyperbolic Functions\# <br> Solutions to Hyperbolic Functions (incl Applications) \# <br> Solve Inequalities involving Hyperbolic Functions\# | Identify Characteristics of Parabolas <br> Relation $y^{\wedge} 2=x$ <br> Graphing Parabolas (based on vertex and transformations) <br> Solve Applications Involving Parabolic Functions <br> General Locus Problems\# |
| Absolute Value Functions | Logarithms | Exponentials |
| Graphing Absolute Value Functions | Revision of Index Laws <br> Logs and Exponential Forms <br> Logarithm Laws and Logarithm Properties <br> Change of Base <br> Evaluating Logarithmic Expressions <br> Identify Characteristics of Logarithmic <br> Functions <br> Transformations of Logarithmic graphs <br> Logarithm Graph <br> Find the Equation of a Logarithm <br> Function\# <br> Evaluate Logarithmic Functions <br> Solving logarithmic equations <br> Applications of Logarithmic Functions <br> Logarithmic Scales <br> Solve Inequalities Involving Logarithmic <br> Functions\# <br> Natural Logarithms <br> Solving Log and Exponential Equations with Technology ${ }^{\#}$ | Identify Characteristics of Exponential <br> Functions <br> Transformations of Exponential graphs <br> Exponential Graph <br> Simplifying Exponential Expressions <br> Transforming Exponential Expressions <br> Finding Exponential Equations in Context <br> Finding Exponential Equations from <br> Graphs or Data <br> Growth and Decay <br> Applications of Exponential Functions <br> Comparing Exponential Models <br> Exponentials VS Linear or Quadratic <br> Functions <br> Evaluating Exponential Functions <br> Solve Exponential Equations <br> Exponential Functions $y=a^{\wedge} x$ Mixed <br> Questions <br> Solve Inequalities Involving Exponential <br> Functions\# <br> Further Exponentials |
| Inverse Functions |  |  |
| Inverse functions <br> Graphs of Inverse Function |  |  |
| Circles |  |  |
| Circles at Origin <br> Circles with translations <br> Circles (Mixed and Semi-Circles) |  |  |
| Combined Conic Sections |  |  |
| Determine Type of Conic Section Identify and Graph Conic Sections\# Find Eccentricity of Conic Section\# |  |  |
| Trig Functions and Graphs | Functions (Graphs and Behaviour) | Polynomials |
| Exact Trigonometric Values <br> Symmetrical and Period Nature of Trig <br> Functions <br> Unit Circle and Trig Functions\# <br> Key Features of Sine and Cosine Curves <br> Transformations of Sine and Cosine <br> Curves and Equations <br> Graphing Sine Curves <br> Graphing Cosine Curves <br> Graphical solution of trig equations\# <br> Applications of Sine and Cosine Functions | Polynomial curve sketching <br> Transformations of Functions <br> Dilation and Symmetry <br> Mixed Graphs I (linear, quad, exp, circles) <br> Mixed graphs II (linear, quad, cubic, $1 / x$ ) <br> Mixed Graphs III (quad, exp, cubic, $1 / x$ ) <br> Comparing Functions (quad, cubic, exp, linear) ${ }^{\#}$ <br> Non-Linear Graphs and Tables of Values <br> Applications of Polynomials <br> Choosing the correct function model <br> Direct and Inverse Variation <br> Using technology to solve problems with graphs I <br> Using technology to solve problems with graphs II <br> Intersections of Graphs by other methods I <br> Intersections of graphs by other methods II | Polynomials and Notation <br> Addition and Subtraction of Polynomials <br> Multiplication of Polynomials <br> Polynomial Division <br> Remainder and Factor Theorem <br> Further applications of remainder and factor theorem <br> Polynomial Division Using Synthetic Division <br> Numerical Approximations of Roots <br> Solving for Zeroes and Coefficients <br> Intermediate Value Theorem ${ }^{\#}$ |


| Sequences and Series | Trigonometry | Circle Geometry |
| :---: | :---: | :---: |
| Introduction to Sequences <br> Introduction to Arithmetic Progressions <br> Recurrence relationships for AP's <br> Terms in Arithmetic Progressions <br> Graphs and Tables - AP's <br> Notation for a Series\# <br> Arithmetic Series (defined limits) <br> Applications of Arithmetic Progressions <br> Introduction to Geometric Progressions <br> Recurrence relationships for GP's <br> Finding the Common Ratio <br> Terms in Geometric Progressions <br> Graphs and Tables - GP's <br> Geometric Series <br> Infinite sum for GP's <br> Applications of Geometric Progressions <br> Applications of Geometric Series\# <br> First Order Linear Recurrences <br> Introduction <br> Graphs and Tables - Recurrence Relations <br> Solutions to Recurrence Relations <br> Applications of Recurrence Relations | The Trigonometric Ratios <br> Triangle Problems <br> Pythagoras in 3D\# <br> Trigonometry in 3D <br> Applications to Real Life <br> Sine Rule <br> Sine Rule (Ambiguous Case) \# <br> Cosine Rule <br> Applications of the Sine Rule <br> Applications of the Cosine Rule <br> Sine and Cosine Rule <br> Area of Non-Right Angled Triangles | Finding angles in Circles <br> Lengths in Circles <br> Parts of Circles <br> Chords of a Circle <br> Arcs, Sectors and Segments of a Circle <br> Cyclic Quadrilaterals <br> Tangents to Circles\# <br> Centres of triangles\# <br> Alternate Segments and Intersecting <br> Chords and Secants\# <br> Proofs using cyclic quadrilaterals\# |
| Probability | Language and Use of Statistics | Univariate Data |
| Experimental Probability <br> Theoretical Probability <br> Relative frequencies of And/Or events <br> Replacement and non-replacement probabilities <br> Identifying Independent and Dependent Events <br> Independent Events <br> Dependent Events <br> Probability of Equally Likely Outcome <br> Mutually Exclusive and Non-Mutually <br> Exclusive Events <br> Conditional Probability - Sample Spaces <br> Bivariate Data <br> Create and Interpret Parallel Box Plots\# <br> Create and Interpret Scatter Plots <br> Describing Statistical Relationships <br> Comparing Sets of Data <br> Comparing Sets of Data II (includes box and whisker) <br> Shape and Correlation of Bivariate Data | Sampling Techniques I <br> Sampling Techniques II <br> Questionnaire design (investigation) <br> Pros and Cons of Samples (Investigation) <br> Conducting a Census (Investigation) <br> Pros and Cons of a Census (Investigation) <br> Statistics in the Media - Misleading <br> (Investigation) <br> Real Life statistics - Society <br> Statistical Investigations (Investigation) <br> Planning a Statistical Investigation II (Investigation) <br> Sources of Bias <br> Sources of Errors\# <br> Misrepresentation of Results\# | Statistical Displays - A review <br> Create and interpret histograms and polygons <br> Create and interpret cumulative frequency tables <br> Create and interpret box and whisker <br> Connecting box and whisker plots and histograms\# <br> Recognising the spread of data <br> Recognising the shape of data <br> Mean <br> Median <br> Mode <br> Range <br> Mean, median mode and range (calculation from graphs and charts) <br> Mean, median mode and range (find missing data) <br> Mean, median mode and range (comparing data sets) <br> Comparisons and Predictions <br> Mean, median, mode and range (combined set) <br> Centre or Spread ? <br> How the shape effects choice of centre and spread <br> Quartiles and Inter-quartile range <br> Quartiles, Deciles and Percentiles <br> 5 Number Summary <br> Using a fence to find Outliers\# <br> Effects of Outliers <br> Variance\# <br> Standard Deviation <br> Applications of Standard Deviation |


| Observing Patterns and Expressing Generally |  |  |
| :---: | :---: | :---: |
| More About Polynomials |  |  |
| manipulate polynomials further including long division up to simple quadratic divisor | Polynomials | Polynomial Division <br> Polynomial Division Using Synthetic Division |
| (NF) recognize the concept of division algorithm | Polynomials | Polynomial Division |
| (NF) understand and use remainder and factor theorems to factorize polynomials up to degree 3 | Polynomials | Remainder and Factor Theorem <br> Further applications of remainder and factor theorem |
| (NF) appreciate the power of factor theorem and also be aware of the limitation of the theorem | Polynomials | Remainder and Factor Theorem Further applications of remainder and factor theorem |
| Arithmetic and Geometric Sequences and their Summation |  |  |
| (NF) explore further the properties of arithmetic and geometric sequences | Sequences and Series | Introduction to Arithmetic Progressions Introduction to Geometric Progressions Introduction to Sequences |
| (NF) develop and use the general terms of the sequences | Sequences and Series | Terms in Arithmetic Progressions <br> Graphs and Tables - AP's <br> Finding the Common Ratio <br> Terms in Geometric Progressions <br> Graphs and Tables - GP's |
| (NF) investigate and use the general formulas of the sum to $n$ terms of arithmetic and geometric sequences | Sequences and Series | Notation for a Series ${ }^{\#}$ <br> Arithmetic Series <br> Geometric Series <br> Applications of Geometric Series\# |
| (NF) develop an intuitive idea on limit and deduce the formula for sum to infinity for certain geometric series | Sequences and Series | Infinite sum for GP's |
| (NF) solve real-life problems such as interest, growth and depreciation, geometric problems etc. | Sequences and Series | Applications of Arithmetic Progressions Applications of Geometric Progressions |
| **explore recurrence in some sequences | Sequences and Series | Recurrence relationships for AP's <br> Recurrence relationships for GP's <br> First Order Linear Recurrences Introduction <br> Graphs and Tables - Recurrence Relations <br> Solutions to Recurrence Relations <br> Applications of Recurrence Relations |

## Algebraic Relations and Functions

| Quadratic Equations in One Unknown |  |  |
| :---: | :---: | :---: |
| formulate and solve quadratic equations by factor method and formula | Quadratic Equations | Identifying Key Features of Quadratics <br> Quadratic relationships <br> Solving basic quadratic equations <br> Solve by Factorisation I \& II <br> Graphing Quadratic Functions in Factorised <br> Form <br> Solving by completing the square I \& II <br> Graphing Quadratic Functions in Turning <br> Point form <br> Using Vertex Formula <br> Solving using the quadratic formula <br> Application Problems with Quadratics <br> Miscellaneous Quadratic Equations <br> NonMonic Quadraitc Equations <br> Graphing Quadratic Functions in General Form |
| solve the equation $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}=0$ by plotting the graph $y=a x^{2}+b x+c$ and reading the $x$-intercepts | Quadratic Equations | Graphing Quadratic Functions in General Form |
| be aware of the approximate nature of the graphical method | Quadratic Equations | Identifying Key Features of Quadratics Quadratic Graphing Review |
| choose the most appropriate strategy to solve quadratic equations | Quadratic Equations | Application Problems with Quadratics Miscellaneous Quadratic Equations Applications of Quadratic Functions using graphs Further Applications |
| recognize the conditions for the nature of roots | Quadratic Equations | The Number and Nature of Solutions Sum and product of roots |
| understand the hierarchy of real-number system and be aware of the characteristics of rational numbers when expressed in decimals | Number and Algebra Review | Recurring Decimals as/from Fractions Converting Recurring Decimals to Fractions |
| More About Equations |  |  |
| (NF) formulate and solve equations which can be transformed into quadratic equations | Quadratic Equations | Variable substitution Method Solve fractional equations that result in quadratics |
| (NF) formulate and solve one linear and one quadratic simultaneous equations by algebraic method | Quadratic Equations | Simultaneous, linear and quadratic equations |
| solve equations by reading intersecting points of given graphs | Functions (Graphs and Behaviour) | Using technology to solve problems with graphs I \& II Intersections of graphs by other methods I \& II |
| appreciate the power and understand the limitation of graphical method in solving equations | Functions (Graphs and Behaviour) <br> Linear Equations II | Using technology to solve problems with graphs I \& II <br> Intersections of graphs by other methods I \& II <br> Linear modelling <br> Linear modelling- Simultaneous Equations Linear Modelling - Break Even Analysis |


| choose the most appropriate strategy to solve equations | Equations <br> Quadratic Equations <br> Cubic Functions Polynomials Linear Equations II <br> Power Functions <br> Hyperbolic Functions <br> Parabolic Functions | Mixed Equations I <br> Mixed Equations II <br> Problem Solving with Linear and Non- <br> Linear Equations <br> Identify Solutions to Linear Equations <br> Solving Cubic Equations <br> Solving Equations through Trial and Improvement <br> Solve Radical Equations <br> Solve Equations with Rational Expressions <br> Solve Equations with Negative Exponents\# <br> Solve Equations with Nested Radicals\# <br> Application Problems <br> Miscellaneous Equations <br> Further Applications <br> Solve applications involving cubic functions <br> Solving for Zeroes and Coefficients <br> Linear modelling <br> Linear modelling- Simultaneous Equations <br> Linear Modelling - Break Even Analysis <br> Solving for Constant of Proportionality in <br> Power Functions <br> Solutions to Hyperbolic Functions (incl Applications)\# <br> Solve Applications Involving Parabolic Functions <br> General Locus Problems\# |
| :---: | :---: | :---: |
| **explore the algebraic method to solve cubic or higher degree equations | Equations Cubic Functions <br> Functions (Graphs and Behaviour) <br> Power Functions | Solving Cubic Equations <br> Solve applications involving cubic functions <br> Graphing Cubic Functions <br> Factoring Cubics with an identifiable factor <br> Polynomial curve sketching <br> Intersections of graphs by other methods I \& II <br> Power Functions |
| Variations |  |  |
| discuss the relations between 2 changing quantities | Linear Equations I <br> Linear Equations II Functions (Graphs and Behaviour) Proportions <br> Inverse Functions | Direct Proportion Inverse Proportion Proportion and Variation Direct and Inverse Variation Proportional Relationships Constant of Proportionality Proportional Relationships as Equations Interpreting Proportional Relationships Graphs and Direct Proportions Direct Proportion Inverse Functions |
| sketch the graphs of direct and inverse variations and recognize the algebraic representations between the quantities | Functions (Graphs and Behaviour) Proportions <br> Inverse Functions | Direct and Inverse Variation <br> Proportional Relationships <br> Constant of Proportionality <br> Proportional Relationships as Equations <br> Interpreting Proportional Relationships <br> Graphs and Direct Proportions <br> Direct Proportion <br> Inverse Functions <br> Graphs of Inverse Functions |

\(\left.$$
\begin{array}{|l|ll|}\hline \begin{array}{l}\text { recognize and appreciate the algebraic } \\
\text { representations of various variations such as } \\
\text { those in the forms of } \mathrm{V}=\pi r^{2} \mathrm{~h} \text { or } \mathrm{y}=\mathrm{k}_{1}+\mathrm{k}_{2} \mathrm{x} \text { etc. }\end{array} & & \text { Proportions }\end{array}
$$ \begin{array}{l}Proportional Relationships <br>
Constant of Proportionality <br>
Proportional Relationships as Equations <br>

Interpreting Proportional Relationships\end{array}\right]\)| Graphs and Direct Proportions |
| :--- |
| Direct Proportion |


| (NF) explore and study the relations between the <br> properties of logarithmic function and that of <br> exponential function |  | Logarithms | Logs and Exponential Forms <br> Evaluating Logarithmic Expressions <br> Evaluate Logarithmic Functions |
| :--- | :--- | :--- | :--- |
| Solving logarithmic equations |  |  |  |
| Solving Log and Exponential Equations with |  |  |  |
| Technology |  |  |  |


| (NF) appreciate the power of the method in generating a perfect square expression | Factorisation <br> Quadratic Equations | Complete the Square <br> Perfect Squares <br> Solving by completing the square I \& II <br> Graphing Quadratic Functions in Turning <br> Point form |
| :---: | :---: | :---: |
| sketch and compare graphs of various types of functions | Functions (Graphs and Behaviour) <br> Quadratics <br> Cubics <br> Power Functions <br> Rational Functions <br> Hyperbolic Functions <br> Parabolic Functions <br> Absoltue Value Functions Logarithms Exponentials <br> Inverse Functions | Mixed Graphs I (linear, quad, exp, circles) <br> Mixed graphs II (linear, quad, cubic, $1 / x$ ) <br> Mixed Graphs III (quad, exp, cubic, $1 / x$ ) <br> Comparing Functions (quad, cubic, exp, linear) \# <br> Non-Linear Graphs and Tables of Values <br> Graphing Quadratic Functions in Factorised <br> Form <br> Graphing Quadratic Functions in Turning <br> Point Form <br> Graphing Quadratic Functions in General Form <br> Quadratic Graphing Review <br> Graphing Cubic Functions <br> Power Functions <br> Identify Characteristics of Simple Rational <br> Functions <br> Graphing Simple Rational Functions <br> Identify Characteristics of Hyperbolic <br> Functions\# <br> Graphing Hyperbolic Functions\# <br> Identify Characteristics of Parabolas <br> Relation $y^{\wedge} 2=x$ <br> Graphing Absolute Value Functions <br> Logarithm Graph <br> Exponential Graph <br> Exponentials VS Linear or Quadratic <br> Functions <br> Graphs of Inverse Functions |
| solve $f(x)>k, f(x)<k, f(x) \geq k, f(x) \leq k$ by reading graphs of $f(x)$ | Inequalities <br> Quadratic Equations Cubic Functions Hyperbolic Functions <br> Logarithms <br> Exponentials | Solve Linear Inequalities from a Graph\# Graphing Linear and Non-Linear Inequalities <br> Solve Quadratic Inequalities\# <br> Solve Inequalities involving Cubics <br> Solve Inequalities involving Hyperbolic <br> Functions\# <br> Solve Inequalities Involving Logarithmic <br> Functions\# <br> Solve Inequalities Involving Exponential Functions\# |
| (NF) explore the effects of transformation on the functions from tabular, symbolic and graphical perspectives | Functions (Graphs and Behaviour) Quadratic Equations <br> Logarithms Exponentials Simple Rational Functions Parabolic Functions <br> Trig Graphs | Dilation and SymmetryTransformations of Functions <br> Transformations and Quadratic Equtions <br> Transformation and Quadratic Graphs <br> Transformations of Logarithmic graphs <br> Transformations of Exponential graphs <br> Transformations of Hyperbolas <br> Graphing Parabolas (based on vertex and transformations) <br> Transformations of Sine and Cosine Curves and Equations |


| (NF) visualize the effect of transformation on the graphs of functions when giving symbolic relations | Functions (Graphs and <br> Behaviour) Quadratic Equations <br> Logarithms Exponentials Simple Rational Functions Parabolic Functions <br> Trig Graphs | Dilation and SymmetryTransformations of Functions <br> Transformations and Quadratic Equtions <br> Transformation and Quadratic Graphs <br> Transformations of Logarithmic graphs <br> Transformations of Exponential graphs <br> Transformations of Hyperbolas <br> Graphing Parabolas (based on vertex and transformations) <br> Transformations of Sine and Cosine Curves and Equations |
| :---: | :---: | :---: |
| Included as background and supporting work |  |  |
| Whilst not explicitly required as part of the curriculum, these subtopics are included for background and supporting work for the benefit it can add to student learning and understanding. | Number and Algebra Review <br> Factorisation <br> Functions (Graphs and Behaviour) Polynomials | Whole Number Review <br> Fraction Review <br> Decimal Review <br> Percentage Review <br> Ratios and Rates Review <br> Algebra Review <br> Probability Review <br> Highest Common Factor <br> Difference of Two Squares <br> Grouping in Pairs <br> Monic Quadratic Trinomials <br> Miscellaneous Factorisations <br> Factorising Algebraic Fractions (mult/div) <br> Factorising Algebraic Fractions (add/sub) <br> Non-Monic Quadratic Trinomials <br> Factoring Sum and Difference of Cubes <br> Applications of Polynomials <br> Choosing the correct function model <br> Numerical Approximations of Roots <br> Intermediate Value Theorem* |

Learning Geometry Through an Intuitive Approach

| Qualitative Treatment of Locus |  |  |
| :---: | :---: | :---: |
| describe verbally or sketch the locus of points moving under a condition or conditions | Combined Conic Sections | Determine Type of Conic Section Identify and Graph Conic Sections\# Find Eccentricity of Conic Section\# Identify Characteristics of Hyperbolic Functions" <br> Graphing Hyperbolic Functions\# Identify Characteristics of Parabolas Relation $\mathrm{y}^{2}=\mathrm{x}$ <br> Graphing Parabolas (based on vertex and transformations) |
| appreciate different conditions which can give rise to the same type of locus | Combined Conic Sections | Determine Type of Conic Section Identify and Graph Conic Sections\# Find Eccentricity of Conic Section ${ }^{\text {\# }}$ Identify Characteristics of Hyperbolic Functions" <br> Graphing Hyperbolic Functions\# Identify Characteristics of Parabolas Relation $\mathrm{y}^{2}=\mathrm{x}$ <br> Graphing Parabolas (based on vertex and transformations) |
| Learning Geometry through a Deductive Approach |  |  |
| Basic Properties of Circles |  |  |
| (NF) understand and use the basic properties of chords and arcs of a circle | Circle Geometry | Lengths in Circles <br> Parts of Circles <br> Chords of a Circle <br> Arcs, Sectors and Segments of a Circle Alternate Segments and Intersecting Chords and Secants ${ }^{\#}$ Centres of triangles\# |
| (NF) understand and use the angle properties of a circle | Circle Geometry | Parts of Circles <br> Finding angles in Circles |
| (NF) understand and use the basic properties of cyclic quadrilateral and tangent to a circle | Circle Geometry | Cyclic Quadrilaterals <br> Tangents to Circles* <br> Proofs using cyclic quadrilaterals\# |
| (NF) appreciate the intuitive and inductive ways of recognizing the properties of circles and see the importance of deductive approach | Circle Geometry | Alternate Segments and Intersecting Chords and Secants ${ }^{\#}$ Proofs using cyclic quadrilaterals\# Centres of triangles" ${ }^{\text {\# }}$ |
| (NF) perform geometric proofs related with circles | Circle Geometry | Alternate Segments and Intersecting Chords and Secants" Proofs using cyclic quadrilaterals\# Centres of triangles\# |
| (NF) appreciate the structure of Euclidean Geometry such as definitions, axioms and postulates etc. and its deductive approach in handling geometric problems | Circle Geometry | Alternate Segments and Intersecting Chords and Secants ${ }^{\#}$ Proofs using cyclic quadrilaterals\# Centres of triangles\# |

Learning Geometry through an Analytic Approach

## Coordinate Treatment of Simple Locus Problems

\(\left.\left.$$
\begin{array}{|l|l|l|}\hline \begin{array}{l}\text { explore and visualize straight line as loci of } \\
\text { moving points and describe the loci with } \\
\text { equations }\end{array} & \text { Linear Equations I } & \text { Identifying key features of Linear functions } \\
\hline \begin{array}{l}\text { recognize the characteristics of equation form } \\
\text { that represents a straight line }\end{array} & & \text { Linear Equations I }\end{array}
$$ \begin{array}{l}Identifying Slope from Equation <br>
Gradient Intercept Form <br>

Equation of a Line: General Form\end{array}\right] $$
\begin{array}{l}\text { The Point Gradient Formula }\end{array}
$$\right]\)| The Two Point Formula |
| :--- |
| Finding the Rule |


| (NF) understand and use the formula $1 / 2 a b \sin C$ and Heron's formula for areas of triangles | Trigonometry | Area of Non-Right Angled Triangles |
| :---: | :---: | :---: |
| (NF) investigate and find the angle between 2 intersecting lines, between a line and a plane, between 2 intersecting planes | Linear Equations II | Angle between two lines\# |
| (NF) apply trigonometric knowledge in solving 2dimensional and 3-dimensional problems | Trig Functions and Graphs Trigonometry <br> Linear Equations II | Applications of Sine and Cosine Functions <br> The Trigonometric Ratios <br> Triangle Problems <br> Trigonometry in 3D <br> Applications of the Sine Rule <br> Applications of the Cosine Rule <br> Sine and Cosine Rule <br> Perpendicular Distance ${ }^{\#}$ |
| Included as background and supporting work |  |  |
| Whilst not explicitly required as part of the curriculum, these subtopics are included for background and supporting work for the benefit it can add to student learning and understanding. | Linear Equations II | Writing Intervals\# Division of an interval in a given ratio |

## Analysis and Interpretation of Data

| Measures of Dispersion |  |  |
| :---: | :---: | :---: |
| recognize range, inter-quartile range and standard deviation as measures of dispersion for a set of data | Univariate Data | Recognising the spread of data <br> Recognising the shape of data <br> Range <br> Centre or Spread ? <br> How the shape effects choice of centre and spread <br> Quartiles and Inter-quartile range Quartiles, Deciles and Percentiles Standard Deviation |
| find range from a given set of data | Univariate Data | Range |
| find inter-quartile range from the cumulative frequency polygon | Univariate Data | Create and interpret histograms and polygons <br> Create and interpret cumulative frequency tables <br> Quartiles and Inter-quartile range |
| construct box-and-whisker diagrams and use them to compare the distributions of different sets of data | Univariate Data <br> Bivariate Data | Create and interpret box and whisker Connecting box and whisker plots and histograms" <br> 5 Number Summary <br> Create and Interpret Parallel Box Plots\# |
| interpret the basic formula of standard deviation and be able to find the standard deviation for both grouped and ungrouped data set | Univariate Data | Standard Deviation Applications of Standard Deviation |
| compare the dispersions of different sets of data using appropriate measures | Univariate Data <br> Bivariate Data | Mean, median mode and range (calculation from graphs and charts) <br> Mean, median mode and range (find missing data) <br> Mean, median mode and range (comparing data sets) <br> Comparisons and Predictions <br> Mean, median, mode and range (combined set) <br> Centre or Spread ? <br> How the shape effects choice of centre and spread <br> Quartiles and Inter-quartile range <br> Create and Interpret Scatter Plots <br> Describing Statistical Relationships <br> Comparing Sets of Data <br> Comparing Sets of Data II (includes box and whisker) <br> Shape and Correlation of Bivariate Data |
| (NF) explore and make conjecture on the effect of the dispersion of the data such as: <br> i. removal of a certain item from the data; <br> ii. adding a common constant to the whole set of data; <br> iii. multiplying the whole set of data by a constant; <br> iv. insertion of zero in the data set. |  | Investigation coming soon |

## Simple Statistical Surveys

| Uses and Abuses of Statistics |  |  |
| :---: | :---: | :---: |
| (NF) recognize different techniques in choosing samples and the criteria in choosing data collection method | Language and Use of Statistics | Sampling Techniques I \& II <br> Conducting a Census (Investigation) <br> Pros and Cons of a Census (Investigation) <br> Sources of Bias <br> Sources of Errors" <br> Misrepresentation of Results\# |
| (NF) investigate methods in which statistical surveys are used and misused in various daily-life activities | Language and Use of Statistics | Sources of Bias <br> Sources of Errors ${ }^{\text {\# }}$ <br> Misrepresentation of Results\# |
| (NF) discuss the strengths and weaknesses of statistical investigations presented in different sources such as news media, advertisements, etc including methods of collecting, presenting and analysing data etc. | Language and Use of Statistics | Statistics in the Media - Misleading (Investigation) <br> Real Life statistics - Society |
| (NF) recognize the complexity in conducting surveys | Language and Use of Statistics | Questionnaire design (investigation) Pros and Cons of Samples (Investigation) |
| Conducting Surveys |  |  |
| **conduct statistical investigations including <br> i. formulating key questions to investigate problems relating to their experience; ii. deciding appropriate data collection method which may involve designing simple questionnaire; <br> iii. applying sampling techniques in collecting data; <br> iv. conducting the investigations; <br> v. making interpretation on the data collected and analyzing their findings; <br> vi. presenting the investigations to other | Language and Use of Statistics | Statistical Investigations (Investigation) Planning a Statistical Investigation II (Investigation) |

## Probability

| More about Probability |  |  |
| :---: | :---: | :---: |
| (NF) recognize the basic laws in probability | Probability | Experimental Probability <br> Theoretical Probability <br> Relatvie frequencies of And/Or events <br> Replacement and non-replacement <br> probabilities <br> Identifying Independent and Dependent <br> Events <br> Independent Events <br> Dependent Events <br> Probability of Equally Likely Outcome <br> Mutually Exclusive and Non-Mutually <br> Exclusive Events <br> Conditional Probability |
| (NF) apply the addition or multiplication laws in a wide variety of activities including real-life problems | Probability | Relatvie frequencies of And/Or events Identifying Independent and Dependent Events <br> Independent Events <br> Dependent Events <br> Conditional Probability |
| (NF) recognize the notion of conditional probability and the notation of $P(A \mid B)$ | Probability | Conditional Probability |

Included as Background and Supporting Work

Whilst not explicitly required as part of the curriculum, these subtopics are included for background and supporting work for the benefit it can add to student learning and understanding

Univariate Data Statistical Displays - A review
Mean
Median
Mode
Using a fence to find Outliers\# Effects of Outliers
Variance ${ }^{\#}$

